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Operator-Based Collapse of Infinite Singularities: Quantum Vacuum Fluctuations across Black Hole Horizons and Big Bang Topological Interfaces

Thomas Weissflog

Department of Physics, Brock University, St. Catharines, Canada

Abstract

Modeling unified field frameworks across shifting gravitational and cosmological boundaries—specifically a 2-dimensional black hole event horizon interface limit (M_2) intersecting a 4-dimensional expanding spacetime center of gravity (M_4) via a 5-dimensional primordial bulk hypervolume (M_5)—generates an infinite hierarchy of mathematical field descriptions when tracking behavior down to infinitely small spacetime singularities ($L \rightarrow 0$). Linear, sequential evaluation of these towers yields divergent unphysical sums and computational intractability. This paper demonstrates how an infinite system of Kaluza-Klein modes, statistical hydrodynamic moments of the early cosmic fluid, and scale-dependent renormalization trajectories can be collapsed into a family of discrete, closed-form invariant constants. We provide a rigorous breakdown of these higher-dimensional structural invariants, detail the mechanism of their geometric infinite origins, and present the master equations required for deployment within physics-informed machine learning architectures.

1. Introduction

A central issue in higher-dimensional geometric models is the behavior of localized fields at the interface of severe gravitational and cosmological boundaries. When a macroscopic vacuum approaches a 2-dimensional black hole event horizon (M_2) as an asymmetric boundary layer, and a primordial cosmic mass center approaches a point source singularity in the 4th dimension (M_4) during the Big Bang epoch, their interaction must be mediated by a 5-dimensional unit hypervolume bulk metric (M_5).

If subatomic particles and high-energy excitations are modeled as localized fields at the intersection of these manifolds, their microscopic states cannot be treated as isolated, finite entities. Instead, they interact with the continuum of modes allowed by the extra dimension, generating an infinite stack of coupling relations. Rather than attempting to compute these relations step-by-step, we isolate the topological and analytic operators that govern the entire continuous spectrum.

2. The Source of Infinity: Asymmetric Boundary Towers

The framework produces three unique infinite hierarchies, each corresponding to a specific physical mechanism within the horizon and cosmological cross-talk matrix:

2.1 The Trans-Planckian Kaluza-Klein Harmonic Tower

When a 5D field equation containing a unit hypervolume parameter ($U_5 = L^5$ or L^4T) wraps around a highly compactified or restricted event horizon boundary interface, it must be expressed via a Fourier series expansion along the fifth coordinate axis y:

$$\Phi(x^{\mu}, y) = \Sigma_{n=-\infty}^{\infty} \varphi_n(x^{\mu}) \exp(i n y / R) \quad (1)$$

Because an infinitely compressed particle at the singularity ($L \rightarrow 0$) possesses a non-zero coupling cross-section to every geometric harmonic mode, the unified field splits into an infinite tower of unique 4D field equations. Each increment of n represents an increasingly massive localized resonant state reflecting trans-Planckian physics.

2.2 The Primordial Hydrodynamic Moment Hierarchy

The micro-states of the turbulent vacuum foam on the 2D horizon sheet or early Big Bang boundary (M_2) are described by statistical distribution functions. Evaluating the transport properties of this extreme plasma requires generating successive moments of the governing kinetic equations:

$$M^{(k)} = \int v^{i_1} v^{i_2} \ldots v^{i_k} f(x, v, t) d^n v \quad (2)$$

Because the localized stresses from the 4D singularity continuously inject energy into the higher-order geometric fluctuations of the 2D sheet, the k-th moment equation remains structurally dependent on the (k+1)-th moment, creating an un-truncated, infinite chain of differential coupling equations.

2.3 Singularity Renormalization Scale Trajectories

As the observation radius approaches the infinitely small limit of a gravitational or cosmic singularity ($L \rightarrow 0$), the running coupling constants g_i scale continuously according to the scale parameter:

$$\mu (d g_i / d \mu) = \beta_i(g_1, g_2, \ldots, g_{\infty}) \quad (3)$$

In a fractal or self-similar higher-dimensional vacuum interface surrounding a black hole or primordial singularity, the number of independent parameters needed to prevent quantum geometric shearing at the point singularity goes to infinity.

3. Collapsing Constants of Infinity

To bypass these uncomputable series, we apply operator and regularization theory to isolate scale-invariant geometric values that act as structural constants of the system.

3.1 The 5D Bulk Geometric Constant (C_5)

The infinite summation of Kaluza-Klein fields at the singularity boundary is structurally constrained by the surface volume of the underlying higher-dimensional unit hypersphere. The spatial integration of the extra dimension yields a rigid geometric constant:

$$C_5 = 8 \pi^2 / 15 \approx 5.2637 \quad (4)$$

This constant represents the exact ratio of the 5D hypervolume boundary to its inner linear axis components. Regardless of how many infinite harmonic modes are generated, their global energy-momentum contribution is bounded by C_5, collapsing the infinite stack into a closed, finite metric modification term.

3.2 The Riemann Zeta Regularization Constant ($\zeta(-1)$)

The zero-point energy sum of the infinite modes of vacuum fluctuations sitting on the M_2 horizon interface is naively divergent:

$$\Xi_{vac} \propto \Sigma_{n=1}^{\infty} n = 1 + 2 + 3 + 4 + ... = \infty \quad (5)$$

By mapping this divergent sequence through a complex analytical contour, we compute its unique, non-trivial analytic continuation via the Riemann Zeta function:

$$\zeta(-1) = -1 / 12 \quad (6)$$

This invariant represents the structural remainder of the infinite continuous space-time fabric under event horizon boundary constraints. It provides the definitive value for calculating the local vacuum pressure acting on a subatomic particle at the brink of the singularity.

3.3 The Asymptotic Safety Fixed Point (g*)

The infinite series of beta functions mapping the renormalization trajectory under a zero-length singularity limit ($L \to 0$) converges onto a non-trivial ultraviolet fixed point:

$$\lim_{\mu\to\infty} \beta_i(g_i) = 0 \Rightarrow g_i \to g_* \quad (7)$$

This fixed point acts as a universal scale-invariant limit, ensuring that as the black hole or Big Bang core collapses to an infinitely small volume, its gravitational and field charges reach a finite ceiling rather than a physical infinity.

4 Unified Cosmic Master Equations

The unified interplay of these three invariants collapses the infinite field dynamics of cosmic and black hole singularities into a highly stable, calculable matrix.

4.1 Geometric Metric Projection Equation

The deformation of the 4D metric $g_{\mu\nu}$ near the gravitational singularity as a function of the 5D hypervolume unit projection is governed by:

$$R_{\mu\nu} - 1/2\, R\, g_{\mu\nu} = C_5 \int_{M_2} [T_{\mu\nu}^{(5)} \cdot \Sigma]\, dA \quad (8)$$

where C_5 scales the net stress-energy tensor projection from the bulk across the horizon boundary.

4.2 Horizon Interface Boundary Tension Equation

The localized energy density of the 2D vacuum interface, under the geometric strain of the 4D cosmic or black hole singularity, is pinned by the regularization constant:

$$\sigma_{interface} = \zeta(-1) \cdot (\hbar\, c / A)\, (\nabla_\mu V \cdot \nabla^\mu T) \quad (9)$$

where the infinite vacuum modes are perfectly stabilized into a finite surface pressure across the event horizon.

4.3 Singularity Mass-Geometric Unification Limit

The effective rest mass m_{eff} of an infinitely small point particle as it reaches the zero-volume Big Bang or black hole singularity is governed by the fixed-point limit:

$$m_{eff} = g_* \oint_{\partial M_5} [U_5 / (A \cdot V \cdot T)]\, d\Omega \quad (10)$$

This confirms that the particle's mass is bounded and topologically determined by the 5D unit space interactions.

4. Conclusion and AI Lab Deployment

This framework establishes that infinite mathematical expressions within black holes and the Big Bang do not imply physical un-quantifiability. By deploying C_5, $\zeta(-1)$, and g^* within computational astrophysics models, the infinite equations are handled natively as an invariant continuum. A specialized laboratory utilizing Physics-Informed Neural Networks (PINNs) can utilize these master equations to bypass brute-force calculation entirely, allowing for exact simulations of boundary-bulk dimensional cross-talk down to the singularity scale.